Animating Human Athletics

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ABSTRACT

This paper describes algorithms for the animation of men and women performing three dynamic athletic behaviors: running, bicycling, and vaulting. We animate these behaviors using control algorithms that cause a physically realistic model to perform the desired maneuver. For example, control algorithms allow the simulated humans to maintain balance while moving their arms, to run or bicycle at a variety of speeds, and to perform a handspring vault. Algorithms for group behaviors allow a number of simulated bicyclists to ride as a group while avoiding simple patterns of obstacles. We add secondary motion to the animations with spring-mass simulations of clothing driven by the rigid-body motion of the simulated human. For each simulation, we compare the computed motion to that of humans performing similar maneuvers both qualitatively through the comparison of real and simulated video images and quantitatively through the comparison of simulated and biomechanical data.

Key Words and Phrases: computer animation, human motion, motion control, dynamic simulation, physically realistic modeling.

INTRODUCTION

People are skilled at perceiving the subtle details of human motion. We can, for example, often identify friends by the style of their walk when they are still too far away to be recognizable otherwise. If synthesized human motion is to be compelling, we must create actors for computer animations and virtual environments that appear realistic when they move. Realistic human motion has several components: the kinematics and dynamics of the figure must be physically correct and the control algorithms must make the figure perform in ways that appear natural. We are interested in the last of these: the design of control strategies for natural-looking human motion.

In particular, this paper describes algorithms that allow a rigid-body model of a man or woman to stand, run, and turn at a variety of speeds, to ride a bicycle on hills and around obstacles, and to perform a gymnastic vault. Figure 1 shows two examples of the animated behaviors. The rigid-body models of the man and woman are realistic in that their mass and inertia properties are derived from data in the biomechanics literature and the degrees of freedom of the joints are chosen so that each behavior can be completed in a natural-looking fashion.

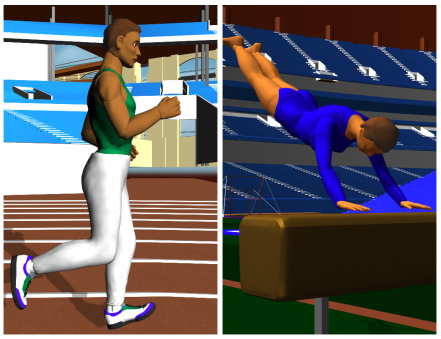

Figure 1: Images of a runner on the track in the 1996 Olympic Stadium and a gymnast performing a handspring vault in the Georgia Dome.

Although the behaviors are very different in character, the control algorithms are built from a common toolbox: state machines are used to enforce a correspondence between the phase of the behavior and the active control laws, synergies are used to cause several degrees of freedom to act with a single purpose, limbs without required actions in a particular state are used to reduce disturbances to the system, inverse kinematics is used to compute the joint angles that would cause a foot or hand to reach a desired location, and the low-level control is performed with proportional-derivative control laws.

We have chosen to animate running, bicycling, and vaulting because each behavior contains a significant dynamic component. For these behaviors, the dynamics of the model constrain the motion and limit the space that must be searched to find control laws for natural-looking motion. This property is most evident in the gymnastic vault. The gymnast is airborne for much of the maneuver, and the control algorithms can influence the internal motion of the joints but not the angular momentum of the system as a whole. The runner, on the other hand, is in contact with the ground much of the time and the joint torques computed by the control algorithms directly control many of the details of the motion. Because the dynamics do not provide as many constraints on the motion, much more effort went into tuning the motion of the runner to look natural than into tuning the motion of the gymnast.

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Computer animations and interactive virtual environments require a source of human motion. The approach used here, dynamic simulation coupled with control algorithms, is only one of several options. An alternative choice, motion capture, is now widely available in commercial software. The difficulty of designing control algorithms has prevented the value of simulation from being demonstrated for systems with internal sources of energy, such as humans. However, simulation has several potential advantages over motion capture. Given robust control algorithms, simulated motion can easily be computed to produce similar but different motions while maintaining physical realism (running at 4 m/s rather than 6 m/s for example). Real-time simulations also allow the motion of an animated character to be truly interactive, an important property for virtual environments in which the actor must move realistically in response to changes in the environment and in response to the actions of the user. And finally, when the source of motion is dynamic simulation we have the opportunity to use multiple levels of simulation to generate either secondary motion such as the movement of clothing and hair or high-level motion such as obstacle avoidance and group behaviors.

BACKGROUND

Research in three fields is relevant to the problem of animating human motion: robotics, biomechanics, and computer graphics. Researchers in robotics have explored control techniques for legged robots that walk, run, balance, and perform gymnastic maneuvers. While no robot has been built with a complexity similar to that of the human body, control strategies for simpler machines provide basic principles that can be used to design control strategies for humanlike models.

Raibert and his colleagues built and controlled a series of dynamic running machines, ranging from a planar machine with one telescoping leg to three-dimensional machines that ran on two or four legs. These machines walked, jumped, changed gait, climbed stairs, and performed gymnastic maneuvers ([14–16], [26–28]). The control algorithms for human running described in this paper build on these control algorithms by extending them for systems with many more controlled degrees of freedom and more stringent requirements on the style of the motion.

Biomechanics provides the data and hypotheses about human motion required to ensure that the computed motion resembles that of a human performing similar maneuvers. The biomechanics literature contains motion capture data, force plate data, and muscle activation records for many human behaviors. These data were used to tune the control algorithms for running, bicycling, and balancing. Cavagna presents energy curves for walking and running as well as studies of energy usage during locomotion[8]. McMahon provides graphs of stance duration, flight duration, and step length as a function of forward speed[21]. Gregor surveys biomechanical studies of bicyclists[13]. Takei presents biomechanical data of elite female gymnasts performing a handspring vault and relates the data to the scores that the gymnasts received in competition[33].

Many researchers in computer graphics have explored the difficult problems inherent in animating human motion. The Jack system developed at the University of Pennsylvania contains kinematic and dynamic models of humans based on biomechanical data[1]. It allows the interactive positioning of the body and has several built-in behaviors including balance, reaching and grasping, and walking and running behaviors that use generalizations of motion capture data[18].

Bruderlin and Calvert used a simplified dynamic model and control algorithms to generate the motions of a walking human[6]. The leg model included a telescoping leg with two degrees of freedom for the stance phase and a compound pendulum model for the swing phase. A foot, upper body, and arms were added to the model kinematically, and were made to move in an oscillatory pattern similar to that observed in humans. Pai programmed a walking behavior for a dynamic model of a human torso and legs in a high-level fashion by describing a set of time-varying constraints, such as, “maintain ground clearance during leg swing,” “lift and put down a foot,” “keep the torso vertical,” and “support the torso with the stance leg” [25].

None of these approaches to generating motion for animation are automatic because each new behavior requires additional work on the part of the researcher. In recent years, the field has seen the development of a number of techniques for automatically generating motion for new behaviors and new creatures. Witkin and Kass[38], Cohen[10], and Brotman and Netravali[5] treat the problem of automatically generating motion as a trajectory optimization problem. Another approach finds a control algorithm instead of a desired trajectory ([37], [36], [23], [31], and [32]). In contrast, the control algorithms described in this paper were designed by hand, using a toolbox of control techniques, our physical intuition about the behaviors, observations of humans performing the tasks, and biomechanical data. While automatic techniques would be preferable to hand design, automatic techniques have not yet been developed that can find solutions for systems with the number of controlled degrees of freedom needed for a plausible model of the human body. Furthermore, although the motion generated by automatic techniques is appealing, much of it does not appear natural in the sense of resembling the motion of a biological system. We do not yet know whether this discrepancy is because only relatively simple models have been used or because of the constraints and optimization criteria that were chosen.

DYNAMIC BEHAVIORS

The motion of each behavior described in this paper is computed using dynamic simulation. Each simulation contains the equations of motion for a rigid-body model of a human and environment (ground, bicycle, and vault), control algorithms for balancing, running, bicycling, or vaulting, a graphical image for viewing the motion, and a user interface for changing the parameters of the simulation. The user is provided with limited high-level control of the animation. For example, the desired velocity and facing direction for the bicyclist and runner are selected by the user. During each simulation time step, the control algorithm computes desired positions and velocities for each joint based on the state of the system, the requirements of the task and input from the user. Proportional-derivative servos compute joint torques based on the desired and actual value of each joint. The equations of motion of the system are integrated forward in time taking into account the internal joint torques and the external forces and torques from interactions with the ground plane or other objects. The details of the human model and the control algorithm for each behavior are described below.

Human Models

The human models we used to animate the dynamic behaviors were constructed from rigid links connected by rotary joints with one, two or three degrees of freedom. The dynamic models were derived from the graphical models shown in figure 2 by computing the mass and moment of inertia of each body part using algorithms for computing the moment of inertia of a polygonal object of uniform density[20] and density data measured from cadavers[11]. We also verified that the model could perform maneuvers that rely on the parameters of the dynamic system using data from Frohlich[12].

The controlled degrees of freedom of the models are shown in figure 2. Each internal joint of the model has a very simple muscle model, a torque source, that allows the control algorithms to apply

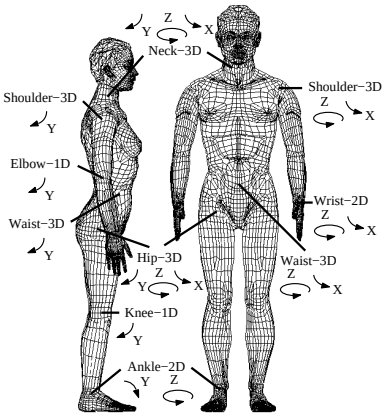

Figure 2: The controlled degrees of freedom of the human model. The gymnast represented in the figure has 15 body segments and a total of 30 controlled degrees of freedom. The runner has 17 body segments and 30 controlled degrees of freedom (two-part feet with a one degree of freedom joint at the ball of the foot and only one degree of freedom at the ankle), The bicyclist has 15 body segments and 22 controlled degrees of freedom (only one degree of freedom at the neck, hips, and ankles). The directions of the arrows indicates the positive direction of rotation for each degree of freedom. The polygonal models were purchased from Viewpoint Datalabs.

a torque between the two links that form the joint. The equations of motion for each system were generated using a commercially available package[30]. The points of contact between the feet and the ground, the bicycle wheels and the ground, and the gymnast's hands and the vault are modeled using constraints. The errors for the constraints are the relative accelerations, velocities, and positions of one body with respect to the other. The constraints are stabilized using Baumgarte stabilization[2].

Running

Running is a cyclic behavior in which the legs swing fore and aft and provide support for the body in alternation. Because the legs perform different functions during the phases of the locomotion cycle, the muscles are used for different control actions at different times in the cycle. When the foot of the simulated runner is on the ground, the ankle, knee, and hip provide support and balance. During the flight phase, a leg is swung forward in preparation for the next touchdown. These distinct phases and corresponding changes in control actions make a state machine a natural tool for selecting the control actions that should be active at a particular time. The state machine and transition events used for the simulation of running are shown in figure 3.

To interact with the animation of the runner, the user specifies desired values for the magnitude of the velocity on the ground plane and the facing direction. The control laws for each state compute joint torques that move the velocity and facing direction toward these desired values while maintaining balance. The animated runner can run at speeds between 2.5 m/s and 5 m/s and runs along a user-defined path.

We call the leg that is on the ground or actively being positioned for touchdown the *active leg.* The other leg is called the *idle leg*. During flight, the active leg is swung forward in anticipation of touchdown. Using the degrees of freedom of the leg in a synergistic fashion, the foot is positioned at touchdown to correct for errors in forward speed and to maintain balance. Forward speed is controlled by placing the average point of support during stance underneath the hip and taking into account the change in contact point from heel to metatarsus during stance. At touchdown, the desired distance from

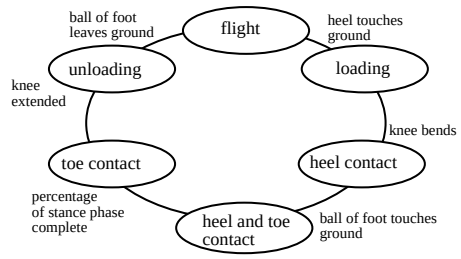

Figure 3: A state machine is used to determine the control actions that should be active for running given the current state of the system. The transition events are computed for the active leg. At liftoff the active and idle legs switch roles. The states correspond to the points of contact on the ground: flight, heel contact, heel and toe contact, and toe contact. The other two states, loading and unloading, are of very short duration and ensure that the foot is firmly planted on the ground or free of the ground before the control actions for stance or flight are invoked.

the hip to the heel projected onto the ground plane is

$$x_{\mathrm{hh}} = 1/2(t_{\mathrm{s}}\dot{x} - \cos(\theta)l_{\mathrm{f}}) + k(\dot{x} - \dot{x}_{\mathrm{d}}) \quad (1)$$

$$y_{\mathrm{hh}} = 1/2(t_{\mathrm{s}}\dot{y} - \sin(\theta)l_{\mathrm{f}}) + k(\dot{y} - \dot{y}_{\mathrm{d}}) \quad (2)$$

where t_{s} is an estimate of the period of time that the foot will be in contact with the ground (based on the previous stance duration), $\dot{x}$ and $\dot{y}$ are the velocities of the runner on the plane, $\dot{x}_{\mathrm{d}}$ and $\dot{y}_{\mathrm{d}}$ are the desired velocities, θ is the facing direction of the runner, l_{f} is the distance from the heel to the ball of the foot, and k is a gain for the correction of errors in speed. The length of the leg at touchdown is fixed and is used to calculate the vertical distance from the hip to the heel, z_{hh}. The disturbances caused by the impact of touchdown can be reduced by decreasing the relative speed between the foot and the ground at touchdown. This technique is called *ground speed matching* in the biomechanical literature. In this control system, ground speed matching is accomplished by swinging the hip further forward in the direction of travel during flight and moving it back just before touchdown.

The equations for x_{hh}, y_{hh}, and z_{hh}, and the inverse kinematics of the leg are used to compute the desired knee and hip angles at touchdown for the active leg. The angle of the ankle is chosen so that the toe will not touch the ground at the same time as the heel at the beginning of stance.

During stance, the knee acts as a passive spring to store the kinetic energy that the system had at touchdown. The majority of the vertical thrust is provided by the ankle joint. During the first part of stance, *heel contact*, the toe moves toward the ground because the contact point on the heel is behind the ankle joint. Contact of the ball of the foot triggers the transition from *heel contact* to *heel and toe contact.* The transition from *heel and toe contact* to *toe contact* occurs when the time since touchdown is equal to a percentage of the expected stance duration (30-50% depending on forward speed). After the transition, the ankle joint is extended, causing the heel to lift off the ground and adding energy to the system for the next flight phase.

Throughout stance, proportional-derivative servos are used to compute torques for the hip joint of the stance leg that will cause the attitude of the body (roll, pitch, and yaw) to move toward the desired values. The desired angle for roll is zero except during turning when the body leans into the curve. The desired angle for pitch is inclined slightly forward, and the desired angle for yaw is set by the user or the higher-level control algorithms for grouping behaviors and obstacle avoidance.

The idle leg plays an important role in locomotion by reducing disturbances to the body attitude caused by the active leg as it swings

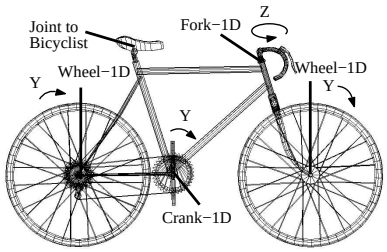

Figure 4: The four degrees of freedom of the bicycle model. The direction of the arrows indicates the positive direction of rotation for each degree of freedom. The polygonal model is a modification of a model purchased from Viewpoint Datalabs.

forward and in toward the centerline in preparation for touchdown. The idle leg is shortened so that the toe does not stub the ground, and the hip angles mirror the motion of the active leg to reduce the net torque on the body:

$$\alpha_{\mathrm{x_d}} = \alpha_{\mathrm{x_{lo}}} - (\beta_{\mathrm{x_d}} - \beta_{\mathrm{x_{lo}}}) \tag{3}$$

$$\alpha_{\mathrm{y_d}} = \alpha_{\mathrm{y_{lo}}} - (\beta_{\mathrm{y_d}} - \beta_{\mathrm{y_{lo}}}) \tag{4}$$

where $\alpha_{\mathrm{x_d}}$ and $\alpha_{\mathrm{y_d}}$ are the desired rotations of the idle hip with respect to the pelvis, $\alpha_{\mathrm{x_{lo}}}$ and $\alpha_{\mathrm{y_{lo}}}$ are the rotation of the idle hip at the previous liftoff, $\beta_{\mathrm{x_d}}$ and $\beta_{\mathrm{y_d}}$ are the desired position of the active hip, and $\beta_{\mathrm{x_{lo}}}$ and $\beta_{\mathrm{y_{lo}}}$ are the position of the active hip at the previous liftoff. The mirroring action of the idle leg is modified by the restriction that the legs should not collide as they pass each other during stance.

The shoulder joint swings the arms fore and aft in a motion that is synchronized with the motion of the legs:

$$\gamma_{\mathrm{y_d}} = k\alpha_{\mathrm{y}} + \gamma_0 \tag{5}$$

where $\gamma_{\mathrm{y_d}}$ is the desired fore/aft angle for the shoulder, k is a scaling factor, α_{y} is the fore-aft hip angle for the leg on the opposite side of the body, and γ_0 is an offset. The other two degrees of freedom in the shoulder (x and z) and the elbows also follow a cyclic pattern with the same period as $\gamma_{\mathrm{y_d}}$. The motion of the upper body is important in running because the counter oscillation of the arms reduces the yaw oscillation of the body caused by the swinging of the legs. However, the details of the motion of the upper body are not constrained by the dynamics of the task and amateur athletes use many different styles of arm motion when they run. Observations of human runners were used to tune the oscillations of the arms to produce a natural-looking gait.

The control laws compute desired values for each joint and proportional-derivative servos are used to control the position of all joints. For each internal joint the control equation is

$$\tau = k(\theta_d - \theta) + k_v(\dot{\theta}_d - \dot{\theta}) \tag{6}$$

The desired values used in the proportional-derivative servos are computed as trajectories from the current value of the joint to the desired value computed by the control laws. Eliminating large step changes in the errors used in the proportional-derivative servos smoothes the simulated motion.

Bicycling

The bicyclist controls the facing direction and speed of the bicycle by applying forces to the handlebars and pedals with his hands and feet. The rider is attached to the bicycle by a pivot joint between the bicycle seat and the pelvis (figure 4). Spring and damper systems connect the hands to the handlebars, the feet to the pedals, and the crank to the rear wheel. The connecting springs are two-sided and the bicyclist is able to pull up on the pedals as if the bicycle were equipped with toe-clips and a fixed gear (no freewheel). The connection between the crank and the rear wheel includes an adjustable gear ratio. The bicycle wheels have a rolling resistance proportional to the velocity.

The control algorithm adjusts the velocity of the bicycle by using the legs to produce a torque at the crank. The desired torque at the crank is

$$\tau_{\mathrm{crank}} = k(v - v_d) \tag{7}$$

where k is a gain, v is the magnitude of the bicyclist's velocity, and v_d is the desired velocity. The force applied by each leg depends on the angle of the crank because we assume that the legs are most effective at pushing downwards. For example, the front leg can generate a positive torque and the rear leg can generate a negative torque when the crank is horizontal. To compensate for the crank position, the desired forces for the legs are scaled by a weighting function between zero and one that depends on the crank position, θ_{crank}:

$$w = \frac{\sin(\theta_{\mathrm{crank}}) + 1}{2}. \tag{8}$$

θ_{crank} is zero when the crank is vertical and the right foot is higher than the left. If $\tau_{\mathrm{crank}} > 0$, the force on the pedal that the legs should produce is

$$f_l = \frac{w\,\tau_{\mathrm{crank}}}{l} \tag{9}$$

$$f_r = \frac{(1-w)\,\tau_{\mathrm{crank}}}{l} \tag{10}$$

where f_l and f_r are the desired forces from the left and right legs respectively, and l is the length of a crank arm. If τ_{crank} is less than zero, then the equations for the left and right leg are switched. An inverse kinematic model of the legs is used to compute hip and knee torques that will produce the desired pedal forces.

To steer the bicycle and control the facing direction, the control algorithm computes a desired angle for the fork based on the errors in roll and yaw:

$$\theta_{\mathrm{fork}} = -k_\alpha(\alpha - \alpha_d) - k_{\dot{\alpha}}\dot{\alpha} + k_\beta(\beta - \beta_d) + k_{\dot{\beta}}\dot{\beta} \tag{11}$$

where α, α_d, and $\dot{\alpha}$ are the roll angle, desired roll, and roll velocity and β, β_d, and $\dot{\beta}$ are the yaw angle, desired yaw, and yaw velocity. k_α, $k_{\dot{\alpha}}$, k_β, and $k_{\dot{\beta}}$ are gains. The desired yaw angle is set by the user or high-level control algorithms; the desired roll angle is zero. Inverse kinematics is used to compute the shoulder and elbow angles that will position the hands on the handlebars with a fork angle of θ_{fork}. Proportional-derivative servos move the shoulder and elbow joints toward those angles.

These control laws leave the motion of several of the joints of the bicyclist unspecified. The wrists and the waist are held at a nearly constant angle with proportional-derivative controllers. The ankle joints are controlled to match data recorded from human subjects[9].

Vaulting and Balancing

To perform a vault, the gymnast uses a spring board to launch herself toward the vaulting horse, pushes off the horse with her hands, and lands on her feet on the other side of the horse. The vault described here, a handspring vault, is one in which the gymnast performs a full somersault over the horse while keeping her body extended in a layout position. This vault is structured by a state machine with six states: hurdle step, board contact, first flight, horse contact, second flight, and landing. The animation of the handspring vault begins during the flight phase preceding the touchdown on the springboard.

The initial conditions were estimated from video footage (forward velocity is 6.75 m/s and the height of the center of mass is 0.9 m).

The simulated gymnast lands on a spring board that deflects based on a linear spring and damper model. When the springboard reaches maximum deflection, the control system extends the knees, pushing on the springboard and adds energy to the system. As the springboard rebounds, it launches the gymnast into the air and the first flight state begins. Using a technique called *blocking*, the control system positions the hips forward before touchdown on the springboard so that much of the horizontal velocity at touchdown is transformed into rotational and vertical velocity at liftoff.

During the first flight state, the control system prepares to put the gymnast's hands on the horse by positioning her shoulders on the line between the shoulders and the desired hand position on the vault:

$$\gamma_{\mathrm{y_d}} = \lambda_{\mathrm{y}} - \phi \tag{12}$$

where $\gamma_{\mathrm{y_d}}$ is the desired shoulder angle relative to the body, λ_{y} is the angle between vertical and a vector from the shoulder to the desired hand position on the vault, and ϕ is the pitch angle of the body (with respect to vertical). Because the shoulders are moving toward the vault during flight, this control law performs ground speed matching between the hands and the horse. The wrists are controlled to cause the hands to hit the horse palm down and parallel to the surface of the horse.

During the next state, the gymnast's hands contact the vault and the arms are held straight. No torque is applied at the shoulder or the wrist and the angular and forward velocity of the gymnast carries her over the horse as she performs the handspring. When the hands leave the vault, the second flight phase begins.

During the second flight state, the control system maintains a layout position with the feet spread slightly to give a larger area of support at touchdown. When the feet hit the ground, the control system must remove the horizontal and rotational energy from the somersault and establish an upright, balanced position. The knees and waist are bent to absorb energy. Vaulters land on soft, 4 cm thick mats that help to reduce their kinetic energy. In our simulation, the behavior of the mat is approximated by reducing the stiffness of the ground. When the simulated gymnast's center of mass passes over the center of the polygon formed by the feet, a balance controller is activated. After the gymnast is balanced, the control system straightens the knees and hips to cause the gymnast to stand up.

The balance controller not only allows the gymnast to stand up after a landing but also compensates for disturbances resulting from the motion of other parts of the body while she is standing. For example, if the gymnast bends forward, the ankles are servoed to move the center of mass of the gymnast backwards. The balance controller also allows the simulated gymnast throw her arms back in a gesture of success after the vault and to take a bow.

HIGHER-LEVEL BEHAVIORS

The control algorithms provide the animator with control over the velocity and facing direction of the runner and bicyclist. However, choreographing an animation with many bicyclists or runners would be difficult because the animator must ensure that they do not run into each other while moving as a group and avoiding obstacles. Building on Reynolds[29], we implemented an algorithm that allows bicyclists to move as a group and to avoid simple configurations of obstacles on the terrain. The performance of the algorithm for a simulation of a bike race on a hill is shown in figure 5.

In contrast to most previous implementations of algorithms for group behaviors, we use this algorithm to control a group where the members have significant dynamics. The problem of controlling these individuals more closely resembles that faced by biological systems because each individual has limited acceleration, velocity, and turning radius. Furthermore, the control algorithms for bicycling are inexact, resulting both in transient and steady-state errors in the control of velocity and facing direction.

The algorithm for group behaviors computes a desired position for each individual by averaging the location and velocity of its visible neighbors, a desired group velocity, and a desired position with respect to the visible obstacles. The details of this computation are presented in Brogan and Hodgins[4]. This desired position is then used as an input to the control algorithm for the bicyclist. The desired position is known only to the individual bicyclist and his navigational intent is communicated to the other cyclists only through their observation of his actions.

The desired position for the bicycle that is computed by the algorithm for group behaviors is used to compute a desired velocity and facing direction:

$$v_{\mathrm{d}} = k_{\mathrm{p}} e + k_{\mathrm{v}}(v_{\mathrm{gl}} - v) \tag{13}$$

where v_{d} is the desired velocity in the plane, v is the actual velocity, e is the error between the current position of the bicyclist and the desired position, k_{p} is the proportional gain on position, k_{v} is the proportional gain on velocity, and v_{gl} is the group's global desired velocity (specified by the user).

SECONDARY MOTIONS

While we are often not consciously aware of secondary motions, they can add greatly to the perceived realism of an animated scene. This property is well known to traditional animators, and much of the work in creating believable hand animation focuses on animating the motion of objects other than the primary actors. This effect can be duplicated in computer animation by identifying the objects in the environment that should exhibit passive secondary behavior and including a simulation suitable for modeling that type of behavior. In some cases, the simulated motion of the passive secondary objects can be driven by the rigid body motion of the primary actors. As examples of this approach, we have simulated sweatpants and splashing water. The behavior of the sweatpants is computed by using the motion of the simulated runner to drive a passive system that approximates the behavior of cloth. Similarly, the motion of splashing water is driven by the motion of a platform diver when it impacts the water ([24] and [35]). Ideally, all objects that do not have active control could be implemented in this fashion. Unfortunately, computational resources and an incomplete understanding of physical processes restrict the size and types of the passive systems that we are able to simulate.

Several methods for physically based animation of cloth have been described in the literature ([7], [22], [3], and [34]). Carignan[7] implemented a system that uses the motion of a kinematic human walker developed by Laurent[19] to drive the action of the cloth. Our approach is similar to that described by Terzopoulos and Fleischer[34]. We use an elastic model to define the properties of the cloth. Collisions are detected using a hierarchical object grouping algorithm and resolved using inverse dynamics to compute reaction forces. Although our cloth model is not significantly different from previous methods, our approach of using dynamically correct rigid body motion to drive the passive system results in an animated scene where all the motion is governed by a consistent set of physically based rules.

DISCUSSION

This paper presents algorithms that allow an animator to generate motion for several dynamic behaviors. Animations of platform diving, unicycle riding and pumping a swing have been described

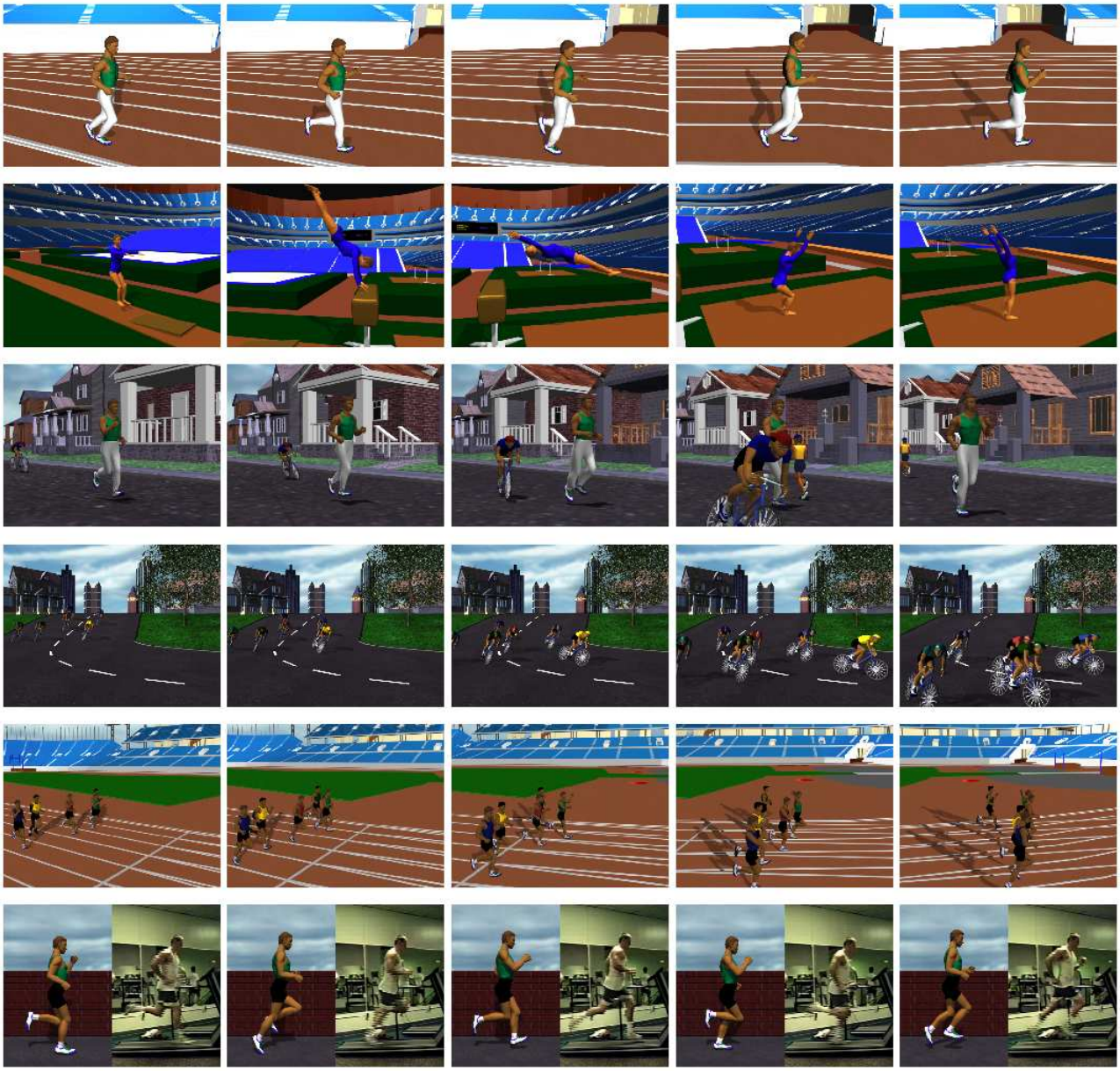

Figure 5: Images of an athlete wearing sweat pants running on a quarter mile track in the 1996 Olympic Stadium, a gymnast performing a handspring vault in the Georgia Dome, a bicyclist avoiding a jogger, a group of bicyclists riding around a corner during a race, a group of runners crossing the finish line, and a comparison between a simulated and a human runner on a treadmill. In each case, the spacing of the images in time is equal with the stadium runner at intervals of 0.066 s, the gymnast at 0.5 s, the single bicyclist at 1.0 s, the group of bicyclists at 0.33 s, the group of runners at 0.5 s and the composite of the simulated and human runner at 0.066 s.

elsewhere ([35], [17]). Taken together with previous work, these dynamic behaviors represent a growing library. While these behaviors do not represent all of human motion or even of human athletic endeavors, an animation package with ten times this many behaviors would have sufficient functionality to be interesting to students and perhaps even to professional animators.

Several open questions remain before the value of simulation as a source of motion for animation and virtual environments can be conclusively demonstrated:

How can we make it easier to generate control algorithms for a new behavior? This paper partially addresses that question by presenting a toolbox of techniques that can be used to construct the control algorithms for a set of diverse behaviors. However, developing sufficient physical intuition about a new behavior to construct a robust control algorithm remains time consuming. We hope that these examples represent a growing understanding of the strategies that are useful in controlling simulations of human motion and that this understanding will lead to the development of more automatic techniques.

What can we do to reduce the number of new behaviors that need to be developed? One idea that has been explored by researchers in the domain of motion capture and keyframing is to perform transitions between behaviors in an automatic or semiautomatic fashion. Such transitions may be much more amenable to automatic design than the design of entire control algorithms for dynamic simulations.

What rules can we add to the system to improve the naturalness of the motion? The techniques presented here are most effective for behaviors with a significant dynamic component because the dynamics constrain the number of ways in which the task can be accomplished. When the gross characteristics of the motion are not constrained by the dynamics of the system, the task can be completed successfully but in a way that appears unnatural. For example, the simulated runner can run while holding his arms fixed at his sides, but an animation of that motion would be amusing rather than realistic. Humans are strong enough and dextrous enough that simple arm movements such as picking up a coffee cup can be completed in many different ways. In contrast, only good athletes can perform a handspring vault and the variations seen in their performances are relatively small. When the dynamics do not significantly constrain the task, the control algorithms must be carefully designed and tuned to produce motion that appears natural while matching the key features of the behavior when performed by a human. The tuning process might be aided by data from psychophysical experiments that would provide additional constraints for the motion.

Can human motion be simulated interactively? To be truly interactive, the motion of synthetic actors in virtual environments must be computed in real time (simulation time must be less than wall clock time). Our implementation of the bicyclist runs ten times slower than real time on a Silicon Graphics Indigo^2 Computer with an R4400 processor. We anticipate that with improved dynamic simulation techniques, and the continued increase in workstation speed, a three-dimensional human simulation will run in real time within a few years.

A related question is whether the behaviors are robust enough for the synthetic actors to interact in a natural fashion with unpredictable human users. The runner can run at a variety of speeds and change direction, but abrupt changes in velocity or facing direction will cause him to fall down. The planning or reactive response algorithms that lie between the locomotion control algorithms and the perceptual model of the simulated environment will have to take in account the limitations of the dynamic system and control system.

One goal of this research is to demonstrate that dynamic simulation of rigid-body models can be used to generate natural-looking motion. Figure 5 shows a side-by-side comparison of video

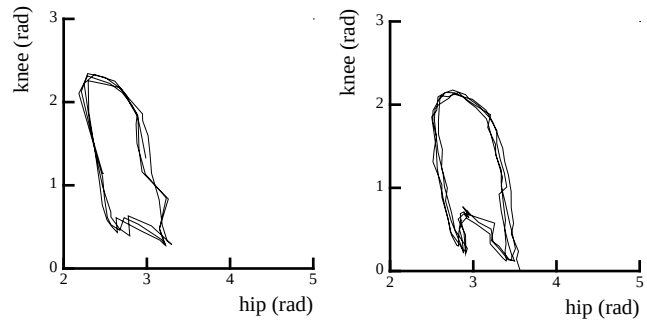

Figure 6: A phase plot of the hip and knee angles seen in the simulated runner (left) and measured in human subjects (right). The simulated motion is qualitatively similar to the measured data.

Variables	Human			Simulation
	Mean	Min	Max	
Mass (kg)	47.96	35.5	64.0	64.3
Height (m)	1.55	1.39	1.66	1.64
Board contact (s)	0.137	0.11	0.15	0.105
First flight (s)	0.235	0.14	0.30	0.156
Horse contact (s)	0.245	0.19	0.30	0.265
Second flight (s)	0.639	0.50	0.78	0.632
Horizontal velocity (m/s)				
Board touchdown	6.75	5.92	7.25	6.75
Board liftoff	4.61	3.97	5.26	4.01
Horse touchdown	4.61	3.97	5.26	4.01
Horse liftoff	3.11	2.48	3.83	2.83
Vertical velocity (m/s)				
Board touchdown	-1.15	-1.54	-.71	-1.13
Board liftoff	3.34	2.98	3.87	3.81
Horse touchdown	1.26	0.74	2.39	2.13
Horse liftoff	1.46	0.56	2.47	1.10
Aver. vertical force (N)				
Board contact	2175	1396	2792	5075
Horse contact	521	309	752	957

Table 1: Comparison of velocities, contact times, and forces for a simulated vaulter and human data measured by Takei. The human data was averaged from 24 subjects. The simulated data was taken from a single trial.

footage of a human runner and images of the simulated runner. This comparison represents one form of evaluation of our success in generating natural-looking motion. Figure 6 shows biomechanical data for running and represents another form of validation. Table 1 compares data from female gymnasts[33] and data from the vault simulation.

From the perspective of computer graphics, the final test would be a form of the Turing Test. If simulated data and motion capture data were represented using the same graphical model, would the audience occasionally choose the simulated data as the more natural motion? The user may find it easy to identify the motion source because motion capture data often has noise and registration problems with limbs that appear to change length and feet that slide on the ground. Simulated motion also has characteristic flaws, for example, the cyclic motion of the runner is repetitive allowing the eye to catch oscillations in the motion that are not visible in the motion of the human runner.

The animations described in this paper and a Turing test comparison with motion capture data can be seen on the WWW at **http://www.cc.gatech.edu/gvu/animation/Animation.html**

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